

**AP CALCULUS AB**  
**Supplement 6.3**  
**Volume by Cross-Sectional Area**

Name \_\_\_\_\_  
Date \_\_\_\_\_  
Period \_\_\_\_\_

1. The base of the solid is the region bounded by  $y = x^2$  and  $y = 2 - x^2$ . Find the volume of the solid if cross sections perpendicular to the  $x$ -axis are (a) squares, and (b) semicircles.
  
2. The base of the solid is the region bounded by  $y = \ln x$ ,  $x = 2$ , and  $y = 0$ . Find the volume of the solid if cross sections perpendicular to the  $y$ -axis are (a) equilateral triangles, and (b) semicircles.
  
3. The base of the solid is the region bounded by  $y = e^{-2x}$ ,  $y = 1$ , and  $x = 3$ . Find the volume of the solid if cross sections perpendicular to the  $y$ -axis are (a) squares, and (b) isosceles right triangles with one leg on the  $xy$ -plane.
  
4. The base of the solid is the region bounded by  $y = x^2$  and  $y = \sqrt{x}$ . Find the volume of the solid if cross sections perpendicular to the  $x$ -axis are (a) equilateral triangles, and (b) isosceles right triangles with one leg on the  $xy$ -plane.

### **Supplement 6.3 Answers**

1a.  $\frac{64}{15}$

1b.  $\frac{8\pi}{15}$

2a. 0.118034

2b. 0.107045

3a. 6.498760

3b. 3.249380

4a.  $\frac{9\sqrt{3}}{280}$

4b.  $\frac{9}{140}$