

3.5 – L'Hôpital's Rule, Part II

Indeterminate Forms

Some common indeterminate forms that often result from direct substitution applied to a limit are:

$$\frac{0}{0}, \frac{\infty}{\infty}, 0 \cdot \infty, \infty - \infty, 0^0, 1^\infty, \infty^0$$

L'Hôpital's Rule

Suppose f and g are differentiable on an open interval containing

a . If direct substitution into $\lim_{x \rightarrow a} \frac{f(x)}{g(x)}$ yields either $\frac{0}{0}$ or $\frac{\infty}{\infty}$, then

$$\lim_{x \rightarrow a} \frac{f(x)}{g(x)} = \lim_{x \rightarrow a} \frac{f'(x)}{g'(x)}$$

Use L'Hôpital's Rule to evaluate the following limits.

1. $\lim_{x \rightarrow 0} \left(\frac{1}{x} - \csc x \right)$

$$2. \lim_{x \rightarrow 1} \left(\frac{1}{\ln x} - \frac{1}{x-1} \right)$$

$$3. \lim_{x \rightarrow 0^+} x^x$$

4. $\lim_{x \rightarrow 0^+} (1 + \sin 4x)^{\cot x}$

5. $\lim_{n \rightarrow \infty} P \left(1 + \frac{r}{n} \right)^{nt}$ (Hint: Apply the constant multiple rule first.)