

**Using derivatives to graph a function without a calculator #1**

$$f(x) = x^5 - 5x^4$$

- a. Find the x intercepts.

$$x^5 - 5x^4 = 0$$

$$x^4(x-5) = 0 \quad x = 0, 5$$

$$(0,0) \quad (5,0)$$

- b. Find the y intercepts.

$$f(0) = 0$$

$$(0,0)$$

- c. Find any asymptotes (horizontal and vertical)

none

- d. Find the end behavior.

$$\lim_{x \rightarrow \infty} f(x) = \infty$$

$$\lim_{x \rightarrow -\infty} f(x) = -\infty$$

- e. Find the first derivative (get a common denominator).

$$f'(x) = 5x^4 - 20x^3$$

- f. Find the critical points. (hint: set numerator=0 and denominator = 0)

$$5x^4 - 20x^3 = 0$$

$$5x^3(x-4) = 0$$

$$x=0 \quad x=4$$

- g. Use the critical points to find any max/mins. (hint: use a sign line)



max at (0,0)

min at (4, -256)

- h. State intervals of increase and decrease.

$f$  is increasing  $(-\infty, 0) \cup (4, \infty)$

$f$  is decreasing  $(0, 4)$

i. Find the second derivative (get a common denominator).

$$f''(x) = 20x^3 - 60x^2$$

j. Find all possible points of inflection. (hint: numer = 0 and denom = 0)

$$20x^2(x-3) = 0$$

$$x=0 \quad x=3$$

$$\text{poi } (3, -162)$$

k. Find intervals of concavity. (hint: use a sign line)



Concave up  $(3, \infty)$

Concave down  $(-\infty, 0) \cup (0, 3)$

l. Sketch the graph of  $f(x)$ . Label intercepts, asymptotes, and max/mins.

