Using derivatives to graph a function without a calculator #4

$$f(x) = (x^2 - 4)^{\frac{2}{3}}$$

- a. Find the x intercepts.
- b. Find the y intercepts
- c. Find any asymptotes (horizontal and vertical)
- d. Find the end behavior.
- e. Find the first derivative (get a common denominator).

f. Find the critical points. (hint: set numerator=0 and denominator = 0)

- g. Use the critical points to find any max/mins. (hint: use a sign line)
- h. State intervals of increase and decrease.

i. Find the second derivative (get a common denominator).

j. Find all possible points of inflection. (hint: numer = 0 and denom = 0)

k. Find intervals of concavity. (hint: use a sign line)

1. Sketch the graph of f(x). <u>Label</u> intercepts, asymptotes, and max/mins.

